Heartbeat Interval Error Compensation Method for Low Sampling Rates Photoplethysmography Sensors*

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SUMMARY This study presents a method for improving the heartbeat interval accuracy of photoplethysmographic (PPG) sensors at ultra-low sampling rates. Although sampling rate reduction can extend battery life, it increases the sampling error and degrades the accuracy of the extracted heartbeat interval. To overcome these drawbacks, a sampling-error compensation method is proposed in this study. The sampling error is reduced by using linear interpolation and autocorrelation based on the waveform similarity of heartbeats in PPG. Furthermore, this study introduces two-line approximation and first derivative PPG (FDPPG) to improve the waveform similarity at ultra-low sampling rates. The proposed method was evaluated using measured PPG and reference electrocardiogram (ECG) of seven subjects. The results reveal that the mean absolute error (MAE) of 4.11 ms was achieved for the heartbeat intervals at a sampling rate of 10 Hz, compared with 1-kHz ECG sampling. The heartbeat interval error was also evaluated based on a heart rate variability (HRV) analysis. Furthermore, the mean absolute percentage error (MAPE) of the low-frequency/high-frequency (LF/HF) components obtained from the 10-Hz PPG is shown to decrease from 38.3% to 3.3%. This error is small enough for practical HRV analysis.

key words: error compensation, heartbeat, heart rate variability analysis, sampling error, photoplethysmography (PPG)

1. Introduction

Daily health monitoring is useful for preventing lifestyle diseases, such as cardiovascular diseases, because it raises health awareness, and lead to improved lifestyle habits [1]. Wearable healthcare devices are important for monitoring daily health. For daily health monitoring, there are various important indicators (e.g., heartbeat, blood pressure, and blood glucose level). Among these indicators, heartbeat is considered a useful biosignal for heart disease detection, exercise intensity estimation [2], and heart rate variability (HRV) analysis [3], [4]. It has been reported that heart rate variability analysis (HRVA) can recognize fatigue and stress conditions [5], and drowsiness and diseases arising from these conditions [6]. For practical use, it is necessary to measure heart rates accurately over a long period. Typically, heartbeat intervals are calculated as R-to-R interval (RRI) of ECG and peak-to-peak interval (PPI) of PPG.

Although ECG can yield more accurate heartbeat intervals, because it directly measures the potential difference on the body surface attributable to the electrical excitation of the heart, it is not suitable for long-term use, because it requires multiple electrodes to be directly attached to the body [8]. In contrast, PPG sensors can efficiently measure heartbeat without electrodes. It irradiates the body’s surface with green or red light, and measures the amount of light absorption by hemoglobin as created by changes in blood volume [9], [10]. There is a few millisecond difference between the heartbeat arrival time of ECG and PPG, because PPG has propagation delay in the blood vessel [11]. However, this difference is not a problem in most applications. Therefore, PPG can easily be implemented in wearable devices such as smartphones, smart bands, and smart rings [12]–[14]. Because the size of the wearable sensors and their battery capacity are strictly limited, it is necessary to reduce power consumption.

There are two major power-consuming components in PPG sensors: LEDs and a wireless data communication circuit (e.g. Bluetooth Low Energy). An effective way of reducing their power consumption is to reduce the activity rate of the LEDs and the amount of transmission data by lowering the sampling rate. However, this leads to a large time error in the extracted heartbeats because of the sampling error; the minimum sampling rate and power reduction efficiency are determined based on the heartbeat accuracy interval required by the application. For instance, an application utilizing heartbeat fluctuation, such as heart rate variability analysis [3], requires that the time error in the heartbeat interval does not exceed a few milliseconds.

To overcome the drawback of sampling-rate reduction methods, we propose an error compensation method based on linear interpolation and autocorrelation using waveform similarity. A preliminary version of this study has been reported in the literature [15]. Although the preliminary study focused on ECG in the performance evaluation, we focus on PPG in this study, because the power consumption of PPG can be reduced more efficiently by sampling rate reduction. Furthermore, this study presents additional error reduction methods; each method is evaluated in detail using seven subjects.

The rest of this paper is structured as follows. Sec-
tion 2 presents the overview of conventional sampling-rate reduction methods for PPG sensors. The proposed sampling error compensation methods are described in Sect. 3. Section 4 presents the experiment results of the proposed methods, which are discussed in Sect. 5. Finally, the conclusions are presented in Sect. 6.

2. Sampling-Rate Reduction Methods for PPG

As mentioned in Sect. 1, reducing the sampling rate is important for reducing the power consumption in PPG sensors. The simplest method is to reduce the overall sampling rate, as shown in Fig. 1(a). Other low sampling-rate-sensing techniques for PPG sensors have been proposed [16], [17].

A parabola approximation method [18] is evaluated to mitigate the sampling error at low sampling rates (see Fig. 1(a)). It is reported that 20-Hz sampled peaks using parabola approximation are comparable to 250-Hz sampled reference signal peaks.

One proposed method uses compressed sampling (CS) technology to reduce the sampling rate to below the Nyquist frequency (see Fig. 1(b)) [16]. The CS method assumes that the PPG signal is sparse in the frequency domain, and performs signal reconstruction on the data of a small number of sample points using matrix operation. In health monitoring applications, the signal reconstruction process can be performed using a server or a gateway (e.g. a smart phone), and the power consumption required for calculation is negligible. However, in this method, because it is impossible to fully reconstruct the original signal, the heartbeat interval error becomes large, resulting in reduced reliability.

In literature [17], a method that samples only the signal around the peak of the PPG waveform to obtain the heartbeat interval is proposed (see Fig. 1(c)). First, two beats extracted from the PPG waveform are sampled to obtain one heartbeat interval. Based on the obtained heartbeat interval, the timing of the detection of the peak of the next PPG waveform is estimated. Sampling commences before the peak, and when the peak is detected, sampling is terminated. Then, the timing of the next peak is estimated again. By restricting the sampling to the vicinity of the peak in this method, the PPG sensor significantly reduces the activity rate of the LED which consumes most of the power. On the other hand, when this method fails to detect a peak, it is necessary to repeat the entire process, and power consumption increases. In particular, the peak detection may fail due to a body motion artifact or arrhythmias, such as extrasystoles, which may occur even in healthy subjects [19].

3. Proposed Sampling Error Compensation Method for Heartbeat Interval Acquisition

Although reducing the sampling rate effectively contributes to power consumption reduction, the heartbeat interval error increases according to the sampling error. Figure 2 shows the PPG waveforms sampled respectively at 1 kHz and 20 Hz. This graph indicates that the interval between peaks, i.e., the heartbeat interval has a large time error corresponding to low sampling rates.

In this study, we propose a sampling error compensation method for the ultra-low sampling-rate condition by incorporating interpolation and autocorrelation into the simple sampling-rate reduction method shown in Fig. 1(a). The proposed method exploits the periodicity and similarity of the heartbeat waveform in PPG. In addition, a waveform-similarity improvement method using the peak waveform approximation and waveform transform is introduced.

3.1 Heartbeat Interval Error Compensation Using Linear Interpolation and Autocorrelation

As shown in Fig. 2, the sampling rate reduction increases the sampling error and decreases the accuracy of the extracted heartbeat interval. Generally, the heartbeat interval is calculated from the peak-to-peak interval of the PPG. In contrast, we introduce a heartbeat interval extraction algorithm based on the similarity of the heartbeat shapes.

Figure 3 shows the flowchart of the proposed method. First, we receive the data sampled by the PPG sensor at a low sampling rate \((F_s)\). Next, the peak of the signal is detected, and linear interpolation and resampling are performed at 1 kHz. The peaks detected at this point are
those for which the sampling error is yet to be compensated (coarse peak detection). Finally, the peak is compensated using the autocorrelation of the waveform near the detected peak, as depicted in Fig. 4. The correlation operation is performed using the following Eq. (1):

$$\text{Cor}(s) = \sum_{j=-\text{win}}^{\text{win}} x(p_n + j)x(p_{n+1} + s + j)$$

Here, $x$ is a zero-normalized input signal; $p_n$ is a peak corresponding to the $n$-th period, $\text{win}$; $\text{win}$ is the window size for autocorrelation; and $s$ is the shift amount of the window. The search window and the template window are the same width, and the search window is shifted closer to the peak. Then, the point with the highest correlation coefficient, that is, the point with the highest similarity to the template window, is designated the compensated peak of the search window corresponding to the peak of the template window. The heartbeat interval is the length of the two peaks following compensation.

Figure 5(a) shows a comparison of the heartbeat intervals with and without the proposed error compensation method. Figure 5(b) shows the relative errors of the heartbeat interval that are calculated from the simultaneously measured reference ECG at a 1-kHz sampling rate. The accuracy of the heartbeat interval at 25-Hz $F_s$ is sufficiently improved by the proposed method, compared to simple peak detection.

3.2 Waveform Similarity Improvement

Next, we introduce a waveform similarity improvement method using two-line approximation. Figure 6 shows the PPG waveform when 10-Hz $F_s$ is superimposed on the 1-kHz PPG waveform and the PPG power spectral density (PSD). As shown in Fig. 6, waveform information such as peaks, is missing at ultra-low sampling rates. Furthermore, due to low waveform similarity, the proposed error compensation described in Sect. 3.1 is not sufficiently effective. Therefore, a pre-processing method for improving the waveform is required prior to error compensation using autocor-
In this study, pre-processing is performed using the two-line approximation, which can improve waveform similarity around peaks. Figure 7 illustrates the outline of this approximation algorithm. Here, we represent the coordinate of the peak as \( P(d, pk) \), and the coordinates on both sides thereof as \( Q(d-1, pr) \), \( R(d+1, ne) \). Then, the time distance of \( \Delta d \) between the detected peak and the new peak is expressed using the following Eq. (2):

\[
\Delta d = \frac{pr - ne}{2(ne - pk)} \quad (pr > ne) \\
\Delta d = \frac{pr - ne}{2(pr - pk)} \quad (pr < ne)
\]

To apply this method to the compensation algorithm described in Sect. 3.1, the new peak obtained using this method and the original sampling point are linearly interpolated along the equiangular lines. Other sampling points besides the peak are interpolated as usual. When using a quadratic function for peak approximation, the \( \Delta d \) is expressed by the following Eq. (3):

\[
\Delta d = \frac{pr - ne}{2(pr + ne) - 4pk}
\]

3.3 Significance of Waveform Characteristics

In this section, we describe the significance of the PPG waveform characteristics on the proposed error compensation. In our preliminary study \([15]\), heartbeat interval compensation algorithm using autocorrelation is applied to the ECG, which has sharper waveforms, compared with PPG (see Fig. 8). Figures 9 and 10 illustrate the correlation operation (1) for the artificial waveform examples assuming PPG and ECG, with and without superimposed noise. The correlation coefficient, calculated by (1), of the steep waveform changes sharply near the peak, while that of the smooth waveform changes gently. Thus, there is the possibility that the desired error compensation effect cannot be achieved due to noise in the situation.

Thus, the dependence of the error compensation efficiency of the proposed error compensation algorithm on the steepness of the peak waveform is a drawback. To mitigate this problem, we use the first derivative of PPG (FDPPG), which has a steep change (see Fig. 11(b)). In addition, because the slope around the peak of FDPPG is symmetrical, the two-line approximation works effectively. Figure 11(c) shows the comparison between PPG and FDPPG PSDs.

Figure 12 illustrates a modified flowchart of heartbeat interval detection from Fig. 3 by adding the two-line approximation algorithm and FDPPG.
4. Performance Evaluation

4.1 Evaluation Methods

To evaluate the performance of heartbeat interval error compensation, 360 seconds duration of PPG and ECG as a reference were synchronously measured from seven subjects (healthy, 21–24 years old male, at rest).

The mean absolute error (MAE) was used to evaluate the heartbeat interval error (4).

\[
MAE = \frac{1}{n} \sum_{i=1}^{n} |PPI_i - RRI_i|
\]  

where \( RRI_i \) is the \( i \)-th heartbeat interval according to the ECG, and \( PPI_i \) is the \( i \)-th heartbeat interval according to the PPG. \( n \) is the number of data.

4.2 Heartbeat Interval

Figure 13 shows the comparison of the heartbeat interval error extracted by the conventional simple peak detection and the proposed error compensation using autocorrelation. Then, the sampling rate of PPG signal is set to 10-Hz Fs. PPG is used in Figs. 13(a) and (c), and FDPPG is used in Figs. 13(b) and (d). Figures 13 (c) and (d) show the results of applying each approximation method to Figs. 13(a) and (b). The combination of error compensation and approximation methods achieves minimum interval error.

Figure 14 shows the average MAE at each sampling rate for all the subjects. A combination of two-line approximation to the FDPPG and compensation using autocorrelation was characterized by less reduction in accuracy when the sampling rate is lowered to 10 Hz. When the sampling rate is 10 Hz, the MAE is 4.11 ms, and the accuracy degradation is only 0.52 ms with respect to the 1-kHz MAE. Figure 15 shows the MAE for each subject at the sampling rate of 10 Hz. The best MAE is exhibited by the autocorrelation method based on the two-line approximation to the FDPPG.

4.3 Heart Rate Variability (HRV) Analysis

In the HRV analysis, changes in heartbeat interval are analyzed in the time and frequency domains [3]. This result can be used for purposes such as heart disease detection and stress monitoring. In this paper, analysis in this study is dominantly performed in the frequency domain. The frequency analysis in the HRV spline interpolates the time series data of the heartbeat interval, and resamples at 4 Hz. Then, the sum of the power spectral density of the low-frequency component (LF) ranging from 0.04 Hz to 0.15 Hz and the high-frequency component (HF) ranging from 0.15 Hz to 0.40 Hz is calculated. The LF, HF, and
LF/HF are generally used as evaluation indexes.

The LF and HF are reflect the sympathetic and parasympathetic nerve activities, respectively. Therefore, LF/HF represents the balance between the sympathetic and parasympathetic nerve activities. A high LF/HF denotes that the sympathetic nervous system has been activated, whereas a low LF/HF signifies that the parasympathetic nervous system has been activated.

Figure 16 shows a sample heartbeat interval and the corresponding result of the HRV analysis. The LF/HF in the heartbeat interval obtained from the ECG at 1 kHz and the PPG at 10 Hz are 1.482 and 0.612, respectively; a large error occurs if compensation is not performed. The LF/HF in the heartbeat interval determined using the autocorrelation of the FDPPG using a two-line approximation was 1.460. The very close results are attributed to the fact that the LF/HF obtained from the 1-kHz PPG is 1.520. Similarly, Table 1 shows the evaluation results of the LF/HF for each subject. Consequently, using the proposed method resulted in improved accuracy for all the subjects, and the mean absolute percentage error (MAPE) was reduced from 38.7% to 3.3%.

### Discussion

The evaluation results in Sect. 4 suggest that the proposed method improves the accuracy at a low sampling rate. However, the peak approximation by the quadratic function at 10 Hz causes accuracy degradation. Nevertheless, the extent of accuracy degradation is reasonable, especially considering the fact that this method is inherently sensitive to noise.

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**Table 1** Comparison of LF/HF in each subject.

<table>
<thead>
<tr>
<th>Subject</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>F</th>
<th>G</th>
</tr>
</thead>
<tbody>
<tr>
<td>ECG at 1 kHz</td>
<td>1.176</td>
<td>0.637</td>
<td>1.887</td>
<td>1.676</td>
<td>0.346</td>
<td>1.482</td>
<td>0.208</td>
</tr>
<tr>
<td>Peak detection at 1 kHz</td>
<td>1.124</td>
<td>0.608</td>
<td>1.861</td>
<td>1.817</td>
<td>0.373</td>
<td>1.398</td>
<td>0.221</td>
</tr>
<tr>
<td>Peak detection at 10 Hz</td>
<td>0.660</td>
<td>0.374</td>
<td>1.363</td>
<td>0.705</td>
<td>0.246</td>
<td>0.612</td>
<td>0.234</td>
</tr>
<tr>
<td>Autocorrelation at 1 kHz</td>
<td>1.214</td>
<td>0.665</td>
<td>1.930</td>
<td>1.816</td>
<td>0.369</td>
<td>1.446</td>
<td>0.223</td>
</tr>
<tr>
<td>Autocorrelation at 10 Hz</td>
<td>1.189</td>
<td>0.685</td>
<td>1.969</td>
<td>1.824</td>
<td>0.380</td>
<td>1.349</td>
<td>0.218</td>
</tr>
<tr>
<td>Prop. at 1 kHz</td>
<td>1.208</td>
<td>0.654</td>
<td>1.929</td>
<td>1.777</td>
<td>0.354</td>
<td>1.520</td>
<td>0.226</td>
</tr>
<tr>
<td>Prop. at 10 Hz</td>
<td>1.192</td>
<td>0.655</td>
<td>1.929</td>
<td>1.766</td>
<td>0.354</td>
<td>1.460</td>
<td>0.224</td>
</tr>
</tbody>
</table>
and such accuracy degradation is obtained at a low sampling rate where the signal-to-noise ratio reduces.

In HRV analysis, some subjects were slightly deteriorated in LF/HF although the accuracy was improved in MAE. This results may caused by the intrinsic difference of LF/HF between PPG and ECG [11], [20], [21].

In this study, we proposed a method that enables the accurate acquisition of heartbeat intervals using PPG at ultra-low sampling rates. This makes it possible to greatly reduce the activity rate of the LEDs, which although being a necessary portion of the PPG measurement, consume power significantly. To illustrate, a previous study [22] measures the PPG at sampling rate of 100 Hz, and found that the LED consumed the most power of all the components of the PPG sensor. By applying the proposed method toward similar end, the power consumption of the LED can be reduced by up to 1/10, that is, it can be reduced from 4400 µW to 440 µW.

Recently, an image PPG (iPPG) using a video camera for non-contact PPG measurement has also been proposed [23]. Because the frame rate of the video camera is generally limited, the proposed method can also be adopted and incorporated into the iPPG to improve the accuracy of the heartbeat interval. On the other hand, because the iPPG uses a non-contact sensor, various noises are easily superimposed on the results, and noise elimination becomes an important issue. Thus, it necessitates the incorporation of a noise removal algorithm, such as that in a prior study [24].

6. Conclusion

We proposed a sampling-rate reduction method based on linear interpolation and autocorrelation for heartbeat interval acquisition using PPG. By applying the proposed method, it is possible to reduce the activity rate of the circuits and LEDs in the PPG sensors, which can contribute to the reduction of power consumption. The results obtained using PPG show that it is possible to reduce the sampling rate to 10 Hz with a MAE of 4.11 ms through a pre-processing method based on two-line approximation and FDPG. In the frequency analysis of the HRV, the LF/HF can be calculated with only 3.3% of the MAPE degradation at 10 Hz.

References


Young Researchers Award.

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